Online Number Theory Seminar

13 January 2023. – 17:00-17:50

Yann Bugeaud: On the continued fraction expansion of algebraic numbers

Let $\xi = [a_0; a_1, a_2, \ldots]$ be an irrational algebraic real number and $(p_k/q_k)_{k\geq 1}$ denote the sequence of its convergents. We survey various (mostly arithmetical) properties of the sequences $(a_j)_{j\geq 1}$ and $(q_k)_{k\geq 1}$. Let $(u_n)_{n\geq 1}$ be a non-degenerate linear recurrence sequence of integers, which is not a polynomial sequence. We show that if the intersection of the sequences $(q_k)_{k\geq 1}$ and $(u_n)_{n\geq 1}$ is infinite, then ξ is a quadratic number, a recent result obtained jointly with Khoa Nguyen.